

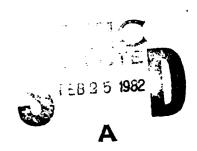


TECHNICAL REPORT RG-81-24

NORTH-FINDING MODULE EVALUATION

S. G. McDaniel H. V. White **Guidance and Control Directorate US Army Missile Laboratory**

April 1981





U.S. ARMY MISSILE COMMAND

Redstone Arsenal, Alabama

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A Litton north-finding module was accuracy and repeatability. Resul	studied to defer	mine its absolute azimuth
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the unit will be used in an in-hou	ise program to der	monstrate its percential as
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CONTENTS

ı.	Introdu	ction	٠.		•			•														•		•	Pag 2	ė
II.	Objecti	ve .	•	•		•		•	•				•	•							•	•	•	•	2	
III.	Procedu	re .		•	•			•			•		•		•	•									2	
IV.	Discuss	ion c	of	Res	su I	lts		•				•		•			•	•		•		•			6	,
v.	Conclus	ion .	•	•				•		•	•								•						6	
	Appendic	es																								
	Α.	Test	P	ro	ced	lur	e					•	•		•						•				7	
	В.	Raw	Da	ta			•								•									•	11	
	С.	Data	R	edu	ıct	io	n	an	ıd	Re	est	11 t	s								•				20	
	D.	Bias	D	ete	ern	nin	at	ic	n																32	





I. INTRODUCTION

The Litton north-finding module (NFM) provides, as its name implies, virtually automatic sensing of true north. The azimuth heading of the NFM is determined by a gyrocompass basically consisting of a Litton G-7 two-degree-of-freedom, dry, tuned-rotor gyro. The NFM uses a normal pendulum configuration with the gyro mounted in a container and suspended by a single metallic wire. This pendulum is enclosed within another container with a fluid used for damping completely filling the space between the two containers.

To achieve useful NFM accuracy for tactical missile aiming, a gyro would normally have to exhibit drift performence of better than 0.005 degree/hr. This is generally exhibited by an inertial navigation grade instrument, whose cost is not compatible with low-cost goals. The simple expedient of rotating the entire sensor assembly 180 and making a second measurement eliminates the day-to-day gyro drift repeatability, hence, a lower cost gyro can be used. For the short NFM measurement times, all but relatively short-term correlated noise and thermal transients due to turn-on are also eliminated. When coupled with the pendulous suspension, it removes any error caused by the gyro horizontal axis not being exactly horizontal.

The rotation of the sensor unit is achieved by a small dc motor that drives the assembly from one stop to another nominally 180° apart. By rotating about the spin axis, this rotation can be made in about 5 seconds without requiring excessive torquing rates from the gyro.

The gyro is pulse-rebalanced, providing output pulses that represent about 0.04 arc second displacement. These pulses are accumulated in an updown counter in such a way that the residual in the counter after two rotations is the difference between the rates measured by the gyro in the 0° and 180° position.

The data in the two registers are processed in a digital computer which contains a 12-bit microprocessor. The microprocessor provides digital filtering of the data and computes the azimuth angle between north and the reference on the NFM case.

Figure 1 shows an outline drawing of the unit. The system block diagram is shown in Figure 2.

II. OBJECTIVE

The object of this study is to evaluate gyrocompass performance of NFM Serial no. 01-100. Gyrocompass performance evaluation includes determination of absolute azimuth accuracy and repeatability.

III. PROCEDURE

The NFM was installed on a mounting stand, Figure 3, by alignment pins and cam locks. The NFM was aligned with the alignment pins and pressed firmly against four mounting pads. The mounting pads were machined so that

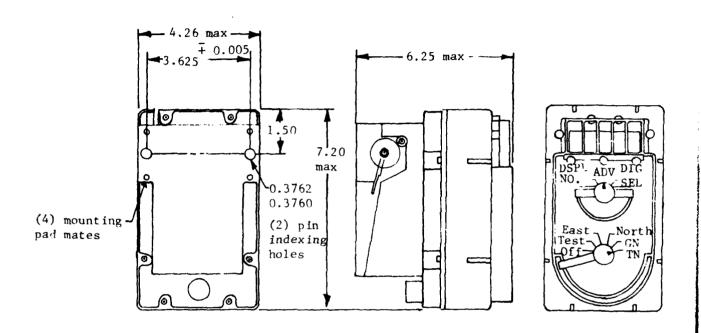


Figure 1. North-finding module.

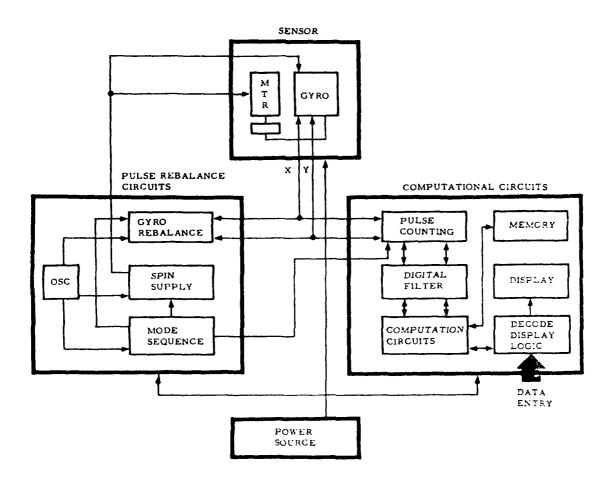


Figure 2. Block diagram of NFM.

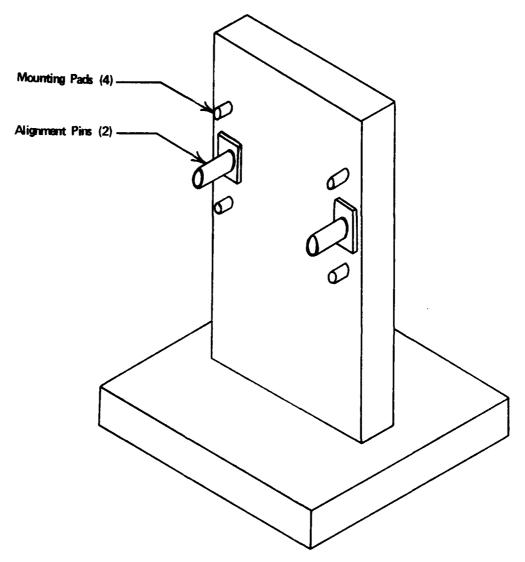


Figure 3. NFM mounting stand.

the plane formed by the pads was perpendicular to the line-of-sight (LOS) of the NFM. The mounting stand was bolted to a Pratt and Whitney 10 in. tilting rotary table.

To obtain the LOS of the NFM, the azimuth of the perpendicular to the plane of the mounting pads was determined. (See Appendix A for azimuth determination.) The rotary table was then set so that the LOS of the NFM was north (0°) . The NFM was energized and initialized so that it gyrocompassed for 3 minutes and 55 seconds. The NFM reading was recorded, and the table was rotated through 45°. This process was repeated eight times after which the table was reset to north (0°) .

The raw data is shown in Appendix B.,

IV. DISCUSSION OF RESULTS

Appendix C shows gyrocompassing results.

A study of the errors shows that, although a bias is evident, the NFM repeats acceptably.

As can be seen in Appendix C the standard deviation is close to the desired 0.25-mil error. Appendix C also shows that with the bias eliminated the root mean square (RMS) error decreases and approaches the one-sigma value which is less than 0.25 mil.

V. CONCLUSIONS

This study shows that, in a laboratory environment, the NFM can determine azimuth heading with reasonable accuracy.

Although the NFM has a bias, this offset can be eliminated electronically, mechanically, or preferably in software. Appendix D shows laboratory bias elimination calculations. With bias elimination, the RMS error is 0.23 mil (Run 3) which points to the possibility of obtaining 0.25 mil in a less benign, field environment.

These results were obtained even though the NFM gyrocompass time was 3 minutes and 55 seconds rather than the allowable goal of 5 minutes. An additional 1 minute of time would be expected to improve results.

The level requirement of $\pm 1/2$ degree would cause problems to a user. The desired goal for field use is $\pm 10^{\circ}$ off-level. This can theoretically be obtained by increasing clearance between the active element and the case. Also, it is expected that desensitization to environmental disturbance would be required for usage in the field.

The unit shows potential for use in an azimuth heading transfer system for tactical missile systems which do not have the on-board capability to self-align. The unit will be utilized in an in-house program to demonstrate this feasibility.

Appendix A TEST PROCEDURE

Gyrocompass accuracy data was acquired using two theodolites, T1 and T2, and the Redstone Arsenal Astro Observation Point Monument, RA. The measurement diagram is shown in Figure A-1 in which the following definitions apply:

- 1) R1 = T1 horizontal scale reading when sighting from T1 to RA
- 2) R2 = T1 horizontal scale reading when sighting from T1 to T2
- 3) R3 = T2 horizontal scale reading when sighting from T2 to T1
- 4) R4 = T2 horizontal scale reading when sighting from T2 to the mounting stand.

Using Figure A-l and the foregoing definitions, the following angles are known or can be calculated as indicated:

- 1) α = known angle between north and LOS to RA, 88° 48' 48"
- 2) $\beta = R2 R1$
- 3) $\zeta = \alpha + \beta$
- 4) $\theta = R4 R3$
- 5) $\Theta = \partial 180^{\circ}$
- 6) $\varepsilon = \zeta + 0$

Entries necessary for calculation of ε were made Data Sheet No. 1.

Optical readings R1, R2, and R3 were determined by the average of two sets of forward and reverse measurements made with the applicable theodolite.

To determine R4, the LOS of the plane formed by the mounting pads had to be determined. This was accomplished with the use of a mirror rigidly attached to a flat plate. The plate was placed on the mounting stand so that it was in intimate contact with the mounting pads. Two sets of forward and reverse measurements were taken, and the average was recorded. The plane, formed by the mounting pads, and the mirror surface were not parallel, so the plate was rotated 180° so that the top of the plate was down. Two sets of forward and reverse measurements were taken and the average recorded.

As can be seen in the raw data in Appendix B, an azimuth difference indeed did occur after the plate was rotated. Figure A-2A shows the azimuth difference, ψ . The actual R4 was determined by bisecting ψ . (See Figure A-2B.) Bisected ψ was calculated by determining the average of the readings with the top of the plate up and the average of the radings with the top of the plate down (R4 readings).

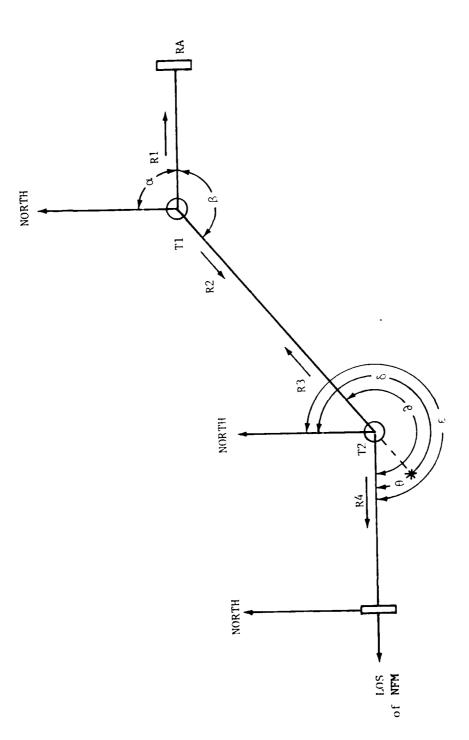


Figure A-1. Optical measurement diagram.

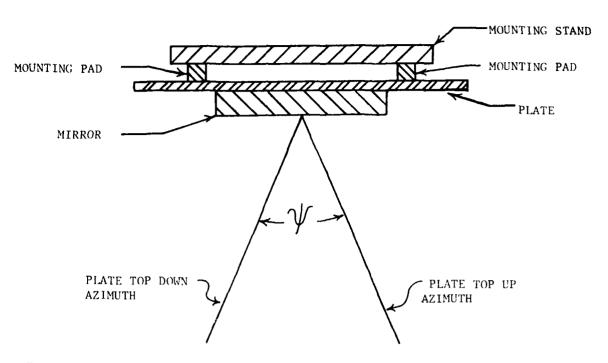


Figure A-2A. Azimuth difference, ψ , occurring when mirror is rotated.

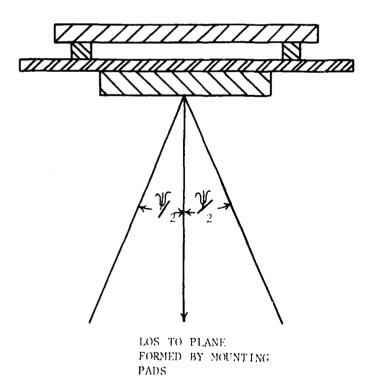


Figure A-2B. LOS to mounting pad plane determined by bisecting ς .

Data Sheet No. 1 AZIMUTH DETERMINATION

Run No.:
T1 S/N:
T2 S/N:
Date :
Optical Data (deg, min, sec)
R2 =

 $R1 = \frac{1}{(\beta = R2 - R1)} : \beta = \frac{\alpha = 088^{\circ} 48^{\circ} 48^{\circ}}{(\zeta = \alpha + \beta)} : \zeta = \frac{1}{(\beta = R2 - R1)}$

 $R4 = \frac{180^{\circ} \ 00^{\circ} \ 00^{\circ}}{10^{\circ} \ 00^{\circ} \ 00^{\circ}}$ $(0 = 3 - 180^{\circ}) : 0 = \frac{180^{\circ} \ 00^{\circ} \ 00^{\circ}}{10^{\circ}}$

 $(\varepsilon = \zeta + \Theta)$: $\varepsilon =$

Appendix B RAW DATA

The following raw data was taken in the Clean Room facility in Building 5400.

Raw optical data (theodolite readings) corresponding to the requirements (minimum of two sets of forward and reverse measurements) of Appendix A are presented in Table B-1. Tables B-2 through B-4 present results of raw data reduction using the optical measurement diagram of Figure A-1, Appendix A.

NFM easting and northing inputs and output data are presented in Tables B-5 through B-8. Predelivery data taken by Litton are included.

TABLE B-1. THEODOLITE READINGS (deg, min, sec)

	n Rev	03 22		03 45	7	04 12	
	Top down	2 165	3 22	5 165	345 03 44	2 332	152 04 13
R4	To	345 03 2	345 03 22 345 05 35	345 03 4	1 345 05 46	152 04 1	2 08
	Top up Rev	165 07 47	345°17 48 345	165 07 49	7 49 345	332 00 05 06	152
	Top	345 07 50	345	345 07 50	345 07 49	152 00 02	152
R3	Rev	159 43 15 339 43 06 157 42 18 337 42 23 345 07 50 165 07 47 345 03 22 165 03 22 165 03 22 165 03 22 22 22 22 22 22 22 22 22 22 22 22 22	157 42 20	159 43 16 339 43 03 157 42 27 337 42 22 345 07 50 165 07 49 345 03 45 165 03 45 44 44 44	157 42 24	159 47 39 339 47 29 132 02 03 312 02 03 152 00 02 332 00 05 152 04 12 332 04 12 41 24 24 00 00 01 04 05 05 05 05 06 05 06 05 06 05 06 05 06 05 06 05 06 05 06 05 06 05 06 05 05 05 05 05 05 05 05 05 05 05 05 05	2 02
	Fwd	157 42 18 17	157	157 42 27 24	157	132 02 03 00	132 02 02
RZ	Rev	339 43 06 07	159 43 11	339 43 03 07	159 43 10	339 47 29 24	7 33
	Fwd	159 43 15 16	159	159 43 16 1 4	159	159 47 39 41	159 47 33
R1	Rev	990 00 23 180 00 22 22 23	000 00 22	*	000 00 22	180 00 21 22	
	Fwd	1) 00 00 23 22	√VG: 000	*	AVG: 000	100 00 27 180 00 21 28	AVG: 000 00 24
Run	ou	-		2		3	

 \star Adverse weather conditions prohibited outside reading. Eighty percent of previous measurements indicate reading of 00° 00' 22"

TABLE B-2. AZIMUTH DETERMINATION

Run No.: 1

T1 S/N: 116699 (Hilgar Watts ST200)

T2 S/N : 55942 (Wild T2)

Date : 23 Mar 81

Optical Data (deg, min, sec)

R2 = 159 43 11

R1 = 000 00 22

 $(\beta = R2 - R1) : \beta = 159 42 49$

 $\alpha = 088 \ 48 \ 48$

 $(\zeta = \alpha + \beta) : \zeta = 248 \ 31 \ 37$

R4 = 345 05 35

R3 = 157 42 20

 $(\partial = R4 - R3) : \partial = 187 23 15$

180 00 00

 $(\Theta = 3 - 180^{\circ}) : \Theta = 007 23 15$

 $\zeta = 248 \ 31 \ 37$

 $(\varepsilon = \zeta + \Theta)$: $\varepsilon = 255$ 54 52

TABLE B-3. AZIMUTH DETERMINATION

Run No.: 2

T1 S/N : 116699 (Hilgar Watts ST200)

T2 S/N: 55942 (Wild T2)

Date : 24 Mar 81

Optical Data (deg, min, sec)

R2 = 159 43 10

R1 = 000 00 22

 $(\beta = R2 - R1) : \beta = 159 42 48$

 $\alpha = 088 \ 48 \ 48$

 $(\zeta = \alpha + \beta) : \zeta = 248 \ 31 \ 36$

R4 = 345 05 46

R3 = 157 42 24

 $(\partial = R4 - R3)$: $\partial = 187 23 22$

180 0000

 $(\Theta = \partial - 180) : \Theta = 007 23 22$

 $\zeta = 248 \ 31 \ 36$

 $(\varepsilon = \zeta + \Theta)$: $\varepsilon = 255$ 54 58

TABLE B-4. AZIMUTH DETERMINATION

Run No.: 3

T1 S/N : 116699 (Hilgar Watts ST200)

T2 S/N: 55942 (Wild T2)

Date : 31 Mar 81

Optical Data (deg, min, sec)

R2 = 159 47 33

R1 = 000 00 24

 $(\beta = R2 - R1) : \beta = 159 47 09$

= 088 48 48

 $(\zeta = \alpha + \beta) : \zeta = 248 35 57$

R4 = 152 02 08

 $R3 = 132 \ 02 \ 02$

(a = R4 - R3) : a = 020 00 06

180 00 00

(0 = 3 - 180) : 0 = -159 59 54

 $\zeta = 248 \ 35 \ 57$

 $(\varepsilon = \zeta + \Theta)$: $\varepsilon = 088$ 36 03

TABLE B-5. NPM OUTPUT DATA

Run No.:	1				‡ ; ;		Date: 23	23 Mar 81	
Easting:	666		Warm-up time:	ime: cord	מרמור				
Northing: 8200	8200								
	ng (m11) (deg)	00.0000	0800.0	1600.00 90	2400.0 135	3200.0 180	4000.00 225	4800.0	5600.0 315
Set No.		,	9 0080	1600.0	2400.4	3200.5	4000.0	6.6627	5600.3
-		0001.3	5.000	1600 1	2400.6	3200.4	4000.1	4800.4	5600.4
2		0000.4	0,000	1 6	0.00%	3200.2	3999.9	4799.9	9.0095
е		0000.5	0800.2	1600.3	2400.3	3200.2	4000.6	4800.0	5600,3
4		0000.5	0799.8	1600.1	2400.3	3200.2	4000.6	4800.0	5600.3
S		0000	0800.5	1599,9	2400.2	3200.1	4000.0	4800.1	5600,4
9 /		00000.3	0800.2	1600.4	2400.3	3200.3	4000.4	4800.0	5600.2

Table entries are in mils

TABLE B-6. NFM OUTPUT DATA

Run No.: 2

Easting: 999

Date:
ld start
time: cold
Warm-up ti
8200
Northing:

Northing:	8200	WE	arm-up tin	Warm-up time: cold start	start	Date:	:: 24 Mar	81	
	Heading (mil) (deg)	0.0000	0800.0	1600.0 90	2400.0 135	3200.0 180	4000.0 225	4800.0	5600.0 315
Set No.		9.0000	0800.4	1600.1	2400.5	3200.0	3999.7	4799.6	5600.1
2		0000.5	0800.4	1600.1	2400.4	3200.3	4000.0	4799.9	5600.3
က		0000.4	0800.5	1600.0	2400.0	3200.8	4000.2	4799.6	5600.2
4		0000.7	0800.0	1599.9	2400.3	3200.2	4000.3	4800.0	5600.2
٧.		7.0000	0800.3	1600.1	2400.3	3200.3	4000.1	4800.1	5600.2
9		0000.4	8.6610	1600.0	2400.3	3200.3	4000.5	4799.5	5599.9
7		0000.3	0800.1	1600.0	2400.3	3200.4	4000.3	4799.7	5600.1
œ		0000.2	9.6640	1599.8	2400.0	3200.0	4000.3	4799.2	5600.2
6		0000.4	0.0080	1600.0	2400.2	3200.1	3999.9	4799.9	5600.0
10		9.0000	0.0080	1600.0	2400.4	3200.1	4000,0	4799.7	5599.9

Table entries are in mils

TABLE B-7. NFM OUTPUT DATA

~			
~			
C			
oN c.			
ç			
•			

Warm-up Lime: בוון אסשבוו המרכי סי יומר סי	able was rotated 30 arc sec to eliminate the bias.
warm-up rime	Note: The table
997	8200
Easting:	Northing:

Warm-up time: 2hr 45min

Date: 31 Mar 81

5600.0 315		5600.0	5599.9	6*6655	5600,2	5599.8
,0 33		,5 56				
4800.0 270		4799.5	4799.9	4799.9	8.6674	4800.0
3200.0 4000.0 180 225		3999.9	3999.9	3999.8	3999.8	4000.0
3200.0 180		3200.2	3200.3	3200.2	3200.1	3199.8
2400.0 135		2400.0	2399.7	2400.0	2400.0	2399.7
1600.0		1599.9	1599.9	1600.2	1600.0	1599.7
0800.0		0800.3	9.0080	0800.4	0.0080	0800.1
0.0000	•	00000.5	0000.4	0000.2	0000.1	0000.1
Heading (mil)						
	Set No.	~	2	က	4	5

Table entries are in mils

TABLE B-8. NFM PREDELIVERY OUTPUT DATA

Date: 11 Mar 81 Easting: 999

Northing: 3782

	Heading (mil) (deg)	0.0000	0800.0 45	1600.0	2400.0 135	3200.0 180	4000.0	4800.0	5600.0 315
Set No.									
н		0000.1	0800.4	1600.2	2400.4	3199.8	3999.9	4799.5	9.0095
2		0000.2	9.0080	1599.9	2400.1	3200.4	4000,1	4799.5	5600.3
ĸ		0000.1	0799.3	1600.2	2400.5	3200.2	4000.7	4800.0	5600.0
4		0000	0.0080	1600.0	2400.3	3200.2	4000.0	4799.3	5600.3

Table entries are in mils

Appendix C DATA REDUCTION AND RESULTS

The error, E, in each gyrocompass run, as shown in Tables C-1 through C-4, was determined by the difference in NFM output, O, and actual heading, AH.

$$E = 0 - AH$$

The root mean square (RMS), mean (\overline{X}) , and standard deviation (σ) of the errors were determined for each heading and each run of each set.

The RMS for each heading, ${\rm RMS}_{\rm h}$, was determined by:

$$RMS_h = \begin{pmatrix} \frac{n}{\Sigma} \\ \frac{i=1}{n} \end{pmatrix}^2 1/2$$
, n = number of readings at a given heading.

The composite RMS for each run, RMS_r , was determined by:

$$RMS_{r} = \left(\frac{\sum_{i=1}^{n} \left(RMS_{h_{i}}\right)^{2}}{n}\right)^{1/2}, n = number of headings = 8.$$

The mean for each heading, \overline{X}_h , was determined by:

$$\overline{X}_h = \frac{\sum_{i=1}^{n} E_i}{n}$$
, $n = number of readings at a given heading.$

The composite mean for each run, \overline{X}_r , was determined by:

$$\overline{X}_r = \frac{\sum_{i=1}^n \overline{X}_{h_i}}{n}$$
, $n = \text{number of headings} = 8$.

The standard deviation for each heading, $\boldsymbol{\sigma}_h$, was determined by:

$$\sigma_{h} = \begin{pmatrix} n & 2 \\ \frac{\Sigma}{1=1} \left(\frac{E_{i} - \overline{X}_{h}}{n-1} \right)^{1/2} \\ n = \text{number of readings at a given heading.} \end{pmatrix}$$

The composite standard deviation for each run, $\boldsymbol{\sigma}_{\boldsymbol{r}}$, was determined by:

$$\sigma_{\mathbf{r}} = \begin{pmatrix} \frac{n}{\Sigma} \left(E_{1} - \overline{X}_{\mathbf{r}} \right)^{2} \\ \frac{1-1}{n-1} \end{pmatrix}^{1/2} , n = \text{total number of readings in a}$$

given run.

The composite randomness for each run, $\mathbf{R}_{\mathbf{r}}$, was determined by:

$$R_{\mathbf{r}} = \begin{pmatrix} \frac{n}{\Sigma} {\sigma_{\mathbf{h}_{\underline{1}}} \choose n}^{2} \end{pmatrix} 1/2$$
, $n = \text{number of headings} = 8$.

The results are shown in Table C-5.

The mean error data contained in Table C-5 are plotted in Figures C-1 through C-4.

Figure C-5 shows histograms of the gyrocompass errors.

TABLE C-1. GYROCOMPASS ERRORS, E

	5600.0 315	0.3	7.0	9.6	0.3	0.3	0.4	0.2
	4800,0 5 270	1 (0.4	1.1	0.0	0.0	0.1	0.0
Mar 81	4000,0 225	0.0	0.1	1.1	9.0	9.0	0.0	9.0
Date: 23 M	3200.0 180	0.5	0.4	0.2	0.2	0.2	0.1	0.3
Da	2400.0 135	0.4			0.3	0.3	0.2	0.3
	1600.0)		, ,		; ;	7.0
	0.0800	}	o 4		7.0	7: 6	2.0	0.2
	0.0000	ο ,	I.3	4.0	0.5	0.5	0.7	0.3
	l Heading (mil)	(geb)						
	Run No.:	Set No.	1	2	٣	4	20	9 ~

Table entries are in mils

TABLE C-2. GYROCOMPASS ERRORS, E

2 Heading (mil)	0000.0 0800.0 1	1600.0	2400.0	Date: 24	24 Mar 81 4000.0	4800.0	5600.0
•		06	cer ,	001	677	0 .	313
9.0		0.1	5.0	0.0	۳ ،	7	0.1
3.5		0.1	0.4	0.3	0.0	1	0.3
7.4	0.5	0.0	0.0	0.8	0.2	4	0.2
2.7		-:1	0.3	0.2	0.3	0.0	0.2
0.7		0.1	0.3	0.3	0.1	0.1	0.2
7.4	2 0	0.0	0.3	0.3	0.5	5:	1
3.3	0.1 0	0.0	0.3	0.4	0.3	٤,	0.1
3.2		2	0.0	0.0	0.3	8.	0.2
5.4	0.0	0.0	0.2	0.1	1	1	0.0
9.6	0.0	0.0	7.0	0.1	0.0	3	1

Table entries are in mils

TABLE C-3. GYROCOMPASS ERRORS, E

	5600.0 315	(0.0	-,1	1.1	0.2	2
	4800.0		2.5	. .1	-,1		0.0
Mar 81	4000.0 225		1	1,1	2	2	0.0
Date: 31 Mar 81	3200.0 180		0.2	0.3	0,2	0.1	-,2
Q	2400.0 135		0.0	٠. ن	0.0	0.0	.3
	1600.0 90		1	1	0.2	0.0	3
	0800.0		0.3	9.0	0.4	0.0	0.1
	0.0000		0.5	0.4	0.2	0.1	0.1
N	Heading (mil) (deg)	Set No.		۱ ،	1 m	, 4	ıς

Table entries are in mils

* This run was made with bias compensation. The bias was removed by rotating the rotary table 30 arc sec. See Appendix B, Table B-7.

TABLE C-4. GYROCOMPASS ERRORS, E

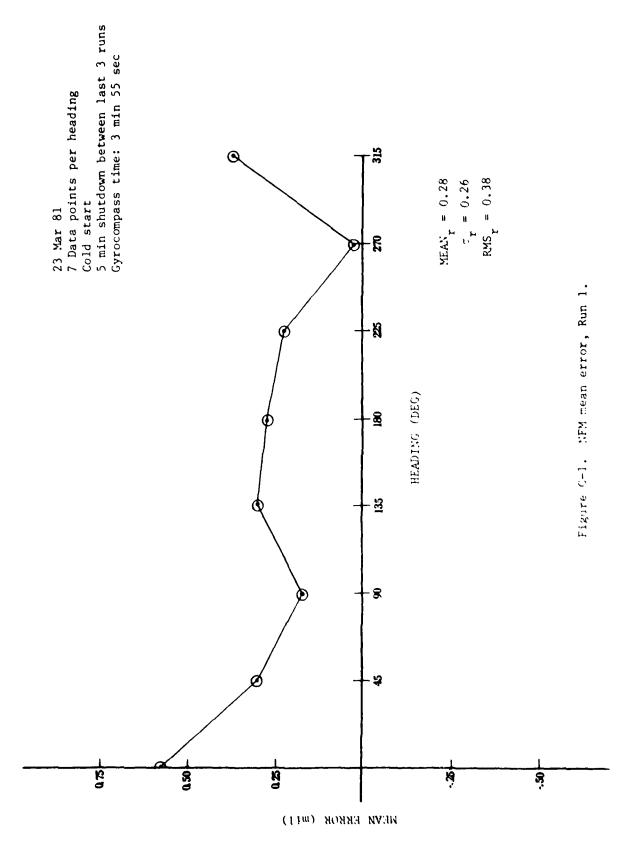
Predeliyery data				Da	Date: li Mar &l	Jar 81		
Heading (mil) (deg)	0. 0000 0	0800.0	1600.0 90	2400.0 135	3200.0 180	4000.0 225	4800.0 270	5600.0 315
Set No.	0.1	7.0	0.2	7.0	2	٠.	٠.5	9.0
2	0.2	9.0	1	0.1	0.4	0.1	5	0.3
en	0.1	7	0.2		0.2	0.7	0.0	0.0
7	0.2	0.0	0.0	0.3	0.2	0.0	۲	0.3

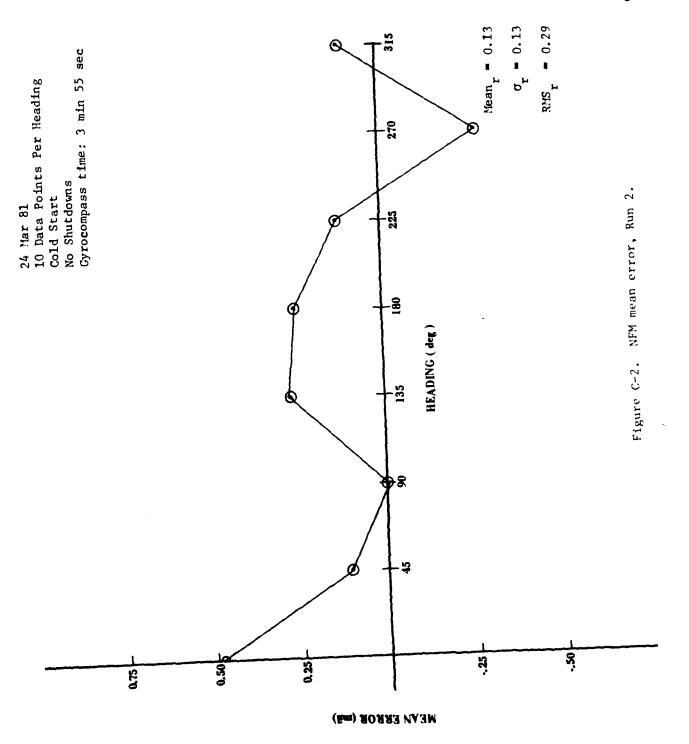
Table entries are in mils

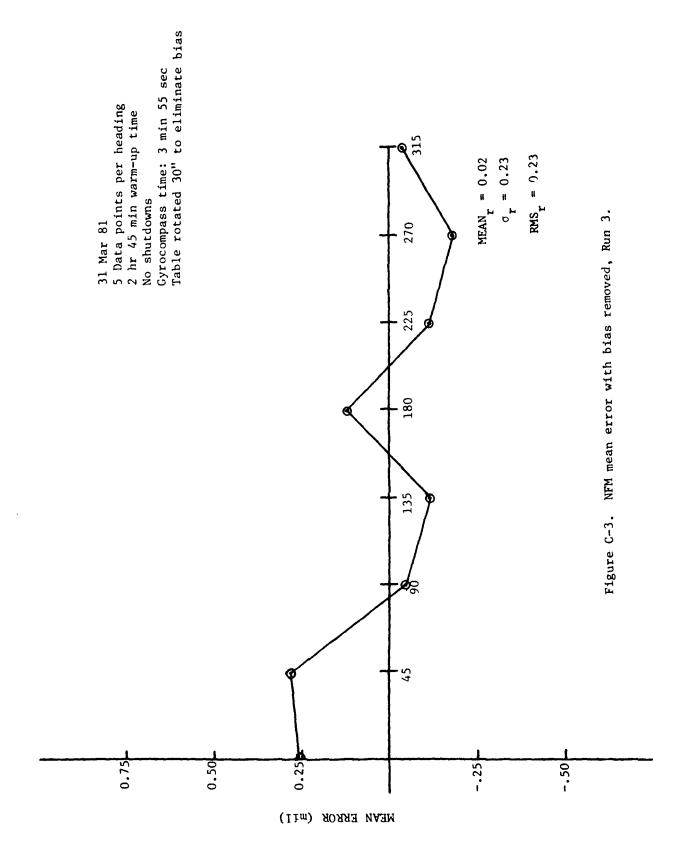
TABLE C-5. GYROCOMPASS TEST RESULTS

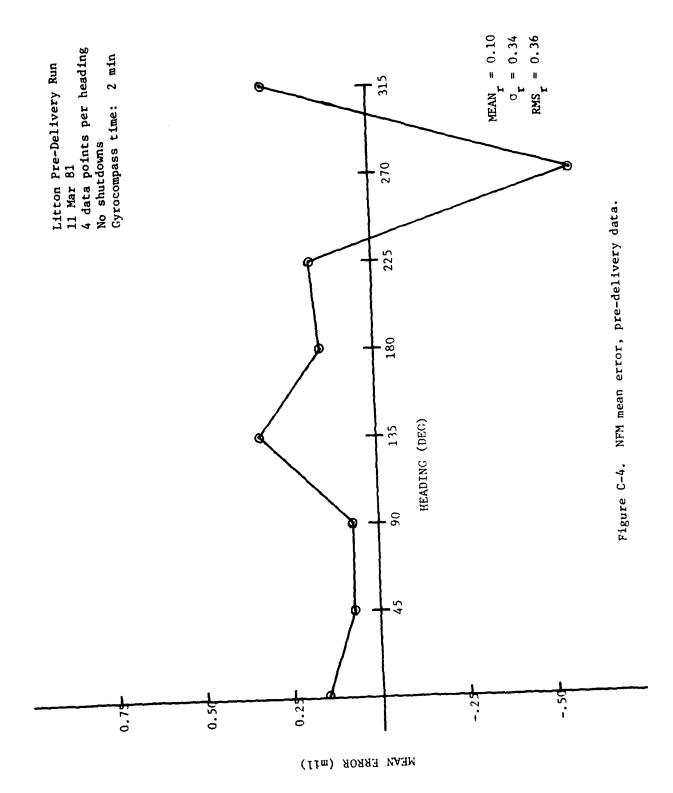
Heading (mil)	Statistic	Run No. 1	Run No. 2	Run No. 3*	Predelivery data
		(mil	s)		
	$\frac{\mathbf{RMS}}{\mathbf{X}}_{\mathbf{h}}$	0.65	0.51	0.31	0.16
0000.0	x _h "	0.57	0.48	0.26	0.15
	$^{\sigma}{}_{ m h}$	0.35	0.17	0.18	0.06
	RMS,	0.40	0.29	0.35	0.50
0800.0	$\overline{\mathbf{x}}_{\mathbf{h}}^{\mathbf{n}}$	0.30	0.11	0.28	0.07
	$\frac{ ext{RMS}}{ ilde{ ilde{X}}_{ ext{h}}}_{ ext{h}}$	0.29	0.29	0.24	0.57
	RMS,	0.25	0.09	0.17	0.15
1600.0	\overline{X}_{h}^{n}	0.17	0.00	-0.06	0.07
	$\frac{\frac{RMS}{X}h}{\sigma_h}$	0.20	0.09	0.18	0.15
	RMS.	0.34	0.31	0.19	0.36
2400.0	\overline{X}_{h}^{n}	0.30	0.27	-0.12	0.33
	$\frac{\underset{\overline{X}}{\text{RMS}}_{h}}{\overset{h}{\sigma_{h}}}$	0.18	0.16	0.16	0.17
		0.30	0.34	0.21	0.26
3200.0	X _h "	0.27	0.25	0.12	0.15
	RMS X h o h	0.14	0.24	0.19	0.25
	R <u>M</u> S _h	0.36	0.26	0.14	0.36
4000.0	х, "	0.23	0.13	-0.12	0.17
	RMS X h oh	0.30	0.24	0.08	0.36
	RMS h	0.16	0.38	0.25	0.50
4800.0	ж _ь "	0.04	-0.28	-0.18	-0.57
	$\overline{\mathbf{x}}_{\mathbf{h}}^{\mathbf{n}}$	0.17	0.27	0.19	0.30
	RMS,	0.38	0.17	0.14	0.37
5600.0	Х _ь "	0.36	0.11	-0.04	0.30
	RMS X h o h	0,13	0.14	0.15	0.24
Composite	$\frac{\text{RMS}}{\overline{X}}_{\mathbf{r}}$	0.38	0.32	0.23	0.36
Statistics	X _r ·	0,28	0.13	0.02	0.10
	$\sigma_{\boldsymbol{r}}^{\boldsymbol{L}}$	0.26	0.29	0.23	0.34
	R _r	0.23	0.21	0.18	0.30

^{*} Run 3 was made with bias removed. See Appendix B, Table B-7.









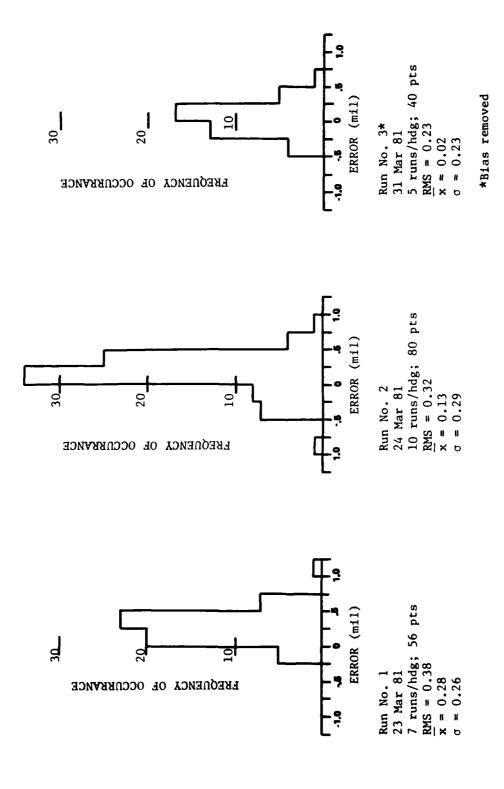


Figure C-5. Histograms of errors.

Appendix D BIAS DETERMINATION

Since Runs 1 and 2 consisted of unequal amounts of data points, a mean bias was determined by an appropriate percentage of each run's mean. Run 1 was weighted by 7/17 and Run 2 was weighted by 10/17. A mean bias, \overline{X}_B , was calculated thusly:

$$\overline{X}_B = \frac{7(0.28 \text{ mil}) + 10(0.13 \text{ mil})}{17} = 0.19 \text{ mil} = 38 \text{ arc sec}$$

A run was made with the rotary table rotated counterclockwise 38 arc sec from true heading but the resulting mean was -0.10 mil, which indicated the table had been rotated too much.

Another run, Run 3, was made with the table rotated 0.15 mil (30 arc sec). The resulting mean was 0.02 mil which indicated that the offset was essentially eliminated.

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